

1. What is the solution set for $x: x^2 + 3x + 2 > 0$?
 - a. $x > -1$
 - b. $x < -2$
 - c. $x > -1$ or $x < -2$
 - d. $x < -1$ and $x > -2$
 - e. $x > -2$
2. If $(e^{2x}) = 3$, then what does e^{6x} equal?
 - a. 6
 - b. 9
 - c. 18
 - d. 27
 - e. 81
3. Which of the following is the equation for the axis of symmetry for $2x^2 - 6x + 5 = y$?
 - a. $x = -6$
 - b. $x = -3$
 - c. $x = -\frac{3}{2}$
 - d. $x = \frac{3}{2}$
 - e. $x = \frac{1}{3}$
4. A two digit number, whose sum of digits is ten, will be 36 less than the original number when the digits are reversed. What is the original number?
 - a. 28
 - b. 37
 - c. 46
 - d. 64
 - e. 73
5. What is the solution set for $2\sqrt{x} = x - 8$?
 - a. $x = 16$ and $x = 4$
 - b. $x = 16$
 - c. $x = 4$
 - d. $x = 16$ and $x = 64$
 - e. $x = 64$
6. What is the value of $9^{-\frac{3}{2}} - 8^{\frac{2}{3}}$?
 - a. $\frac{1}{72}$
 - b. $-\frac{1}{72}$
 - c. $-\frac{4}{27}$
 - d. $\frac{1}{27}$
 - e. -108

7. What is the remainder after dividing $2x^2 - x + 2 \overline{)8x^4 + 6x^2 - 3x + 1}$?
- $-x - 1$
 - $-7x + 1$
 - $-7x - 1$
 - $5x + 1$
 - $5x - 1$
8. Which is the value of $(6 + 3i)^{-1}$, in $a + bi$ form, without exponents?
- $-6 - 3i$
 - $\frac{1}{6} + \frac{1}{3}i$
 - $\frac{15}{2-i}$
 - $\frac{9}{2-i}$
 - $6 - 3i$
9. A third degree equation with rational coefficients has $x = -2$ and $x = 1 + 2i$ as roots. Which is this polynomial with lowest coefficients?
- $x^3 - 4x^2 - 3x + 18$
 - $x^3 - 8x^2 + 21x - 18$
 - $x^3 - x + 6$
 - $x^3 + x + 10$
 - $x^3 + 2x^2 + x + 2$
10. Which is the solution for x : $\log(x + 4) + \log(x + 1) = 1$?
- $x = 1$
 - $x = -6$
 - $x = 1$ or $x = -6$
 - $x = -3$ or $x = 0$
 - $x = 0$

Answers

- C. When working with quadratic inequalities, it is first necessary to factor the quadratic. $x^2 + 3x + 2 > 0$ becomes $(x + 2)(x + 1) > 0$. A product of two numbers can only be positive when the factors are either both positive or both negative.
 - For both factors to be positive: $x + 2 > 0$ AND $x + 1 > 0$. That is, $x > -2$ AND $x > -1$. For both of these conditions to be met, x must be greater than -1 .
 - For both factors to be negative: $x + 2 < 0$ AND $x + 1 < 0$. That is, $x < -2$ AND $x < -1$. For both of these conditions to be met, x must be less than -2 .
 - The solution set is, therefore, $x > -1$ OR $x < -2$.

2. D. Given $(e2x) = 3$. Since $(an)^m = anm$, $e6x$ can be re-written as $(e2x)^3$ or 3^3 which equals 27.
3. D. The equation for the axis of symmetry for a quadratic, $ax^2 + bx + c = y$, is $x = -\frac{b}{2a}$. In $2x^2 - 6x + 5 = y$, $a = 2$, $b = -6$ and $c = 5$. Therefore, the axis of symmetry is $x = 1.5$.
4. E. Let $t =$ the ten's digit number and $u =$ the unit's digit number.
- a. Sum of the digits is 10: $t + u = 10$

The value of the original number can be found by $10t + u$ The value of the reversed digits number can be found by $10u + t$

- b. The original number minus the reversed number is 36: $(10t + u) - (10u + t) = 36$ or $9t - 9u = 36$. Divide both sides of the equation by 9 to obtain $t - u = 4$. Taking $t + u = 10$ from (1) above, add both equations to obtain $2t = 14$ or $t = 7$. That is, the ten's digit is 7. The unit's digit must be 3 (their sum is 10). Therefore, the original number is 73.
5. B. Square both sides of the equation $2\sqrt{x} = x - 8$ to obtain $4x = x^2 - 16x + 64$ or

$0 = x^2 - 20x + 64$. Factor the quadratic: $0 = (x - 4)(x - 16)$, $x = 4$ or $x = 16$. You MUST check both results.

$x = 4$: $2\sqrt{4} = 4 - 8$ yields $4 = -4$, which is untrue. Therefore, $x = 4$ is not a viable solution. This is called an "extraneous" solution.

$x = 16$: $2\sqrt{16} = 16 - 8$ or $8 = 8$, which is true. Therefore, $x = 16$ is correct.

6. C. To find the value of $\sqrt{16}$ or $\sqrt{64}$, evaluate $\sqrt{16}$ and $\sqrt{64}$, separately: $\sqrt{16} = 4$ or $\sqrt{64} = 8$

Multiply $\sqrt{16} \times 4$ to obtain the answer, $\sqrt{64} = 8$.

7. B. To find the quotient: $2x^2 - x + 2 \overline{) 8x^4 + 0x^3 + 6x^2 - 3x + 1}$,

NOTE: All terms, starting with degree 4, must be included in the dividend, hence the insertion of $0x^3$. Now, take the highest degree term in the divisor, $2x^2$, to divide into the highest degree term in the dividend, $8x^4$, to obtain $4x^2$:

$$2x^2 - x + 2 \overline{) 8x^4 + 0x^3 + 6x^2 - 3x + 1}, \text{ multiply divisor by } 4x^2$$

$-(8x^4 - 4x^3 + 8x^2)$ subtract

$4x^3 - 2x^2 - 3x$ divide $2x^2$ into $4x^3$ to obtain $2x$

$-(4x^3 - 2x^2 + 4x)$ subtract

$-7x + 1$ this is the remainder (since $2x^2$ is a higher degree than $-7x$)

8. C. $(6 + 3i)^{-1} = \frac{1}{6 + 3i}$. Correct form would eliminate the “ i ” from the denominator. To have the fraction in correct form, multiply numerator and denominator by the complex conjugate of the denominator, which is $6 - 3i$.

$$\frac{1}{6 + 3i} \cdot \frac{6 - 3i}{6 - 3i} = \frac{6 - 3i}{36 - 9i^2} \text{ or } \frac{6 - 3i}{36 - 9(-1)} = \frac{6 - 3i}{45}$$

Since all three parts are divisible by 3, divide each part by three to obtain: $\frac{2 - i}{15}$

9. D. Since the coefficients are rational and one root, $1 + 2i$, is complex, another root must be its complex conjugate or $1 - 2i$. To find the polynomial, multiply the following:

$(x + 2)(x - [1 + 2i])(x - [1 - 2i])$. To make this process efficient, multiply the last two factors first:

$$(x - [1 + 2i])(x - [1 - 2i]) = x^2 - x[1 - 2i] - x[1 + 2i] - [1 + 2i][1 - 2i] \text{ or}$$

$$x^2 - x + 2xi - x - 2xi + 1 - 2i + 2i - 4i^2 \text{ or}$$

$$x^2 - 2x + 1 - 4(-1) \text{ or } x^2 - 2x + 5$$

Now, multiply $(x + 2)(x^2 - 2x + 5) = x^3 - 2x^2 + 5x + 2x^2 - 4x + 10$ or $x^3 + x + 10$.

10. A. In $\log(x + 4) + \log(x + 1) = 1$, first recognize that the sum of logs means the two values are multiplied or $\log(x + 4)(x + 1) = 1$ (since $\log a + \log b = \log ab$).

Now, $\log x = a$ is equivalent to $10^a = x$: $(x + 4)(x + 1) = 10$ or $x^2 + 5x + 4 = 10$

Subtract 10 from both sides: $x^2 + 5x - 6 = 0$

Factor: $(x - 1)(x + 6) = 0$ or $x = 1$, $x = -6$

If $x = -6$, the value of the numbers in the log function, $x + 4$ and $x + 1$, will be negative, which is not possible because the value placed in a log MUST be positive. Therefore, the only solution is $x = 1$.

