

General Certificate of Secondary Education June 2011

Methods in Mathematics (Pilot)
93651F
(Specification 9365)
Unit 1: Methods in Mathematics Written Paper (Foundation)

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## Glossary for Mark Schemes

GCSE examinations are marked in such a way as to award positive achievement wherever possible. Thus, for GCSE Mathematics papers, marks are awarded under various categories.

M Method marks are awarded for a correct method which could lead to a correct answer.

A Accuracy marks are awarded when following on from a correct method. It is not necessary to always see the method. This can be implied.

B Marks awarded independent of method.
Q Marks awarded for quality of written communication. (QWC)
M Dep A method mark dependent on a previous method mark being awarded.

BDep A mark that can only be awarded if a previous independent mark has been awarded.
ft Follow through marks. Marks awarded following a mistake in an earlier step.

SC Special case. Marks awarded within the scheme for a common misinterpretation which has some mathematical worth.
oe Or equivalent. Accept answers that are equivalent. eg, accept 0.5 as well as $\frac{1}{2}$

## M1 Foundation Tier

## Section A

| $\mathbf{Q}$ | Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |


| 1(a) | $\frac{1}{4}$ | B1 |  |
| :---: | :--- | :---: | :--- |
| $\mathbf{1 ( b ) ~}$ | $1 \frac{1}{2}$ | B1 |  |
| $\mathbf{1 ( c )}$ | $\frac{3}{4}$ | B1 | 0.75 |
| $\mathbf{1 ( d )}$ | Between $1 \frac{1}{4}$ and $1 \frac{1}{2}$ | B1 |  |
| $\mathbf{1 ( e ) ~}$ | 0.125 | B1 |  |


| $\mathbf{2}$ | $(0) .6(0) \times 2(=1.20)$ | M1 | $60 \times 2(=120)$ |
| :---: | :--- | :---: | :--- |
|  | $4-$ their $1.2(0)(=2.8(0))$ | M1 | $400-$ their $120(=2.80)$ |
|  | Their $2.8(0) \div 4(=0.70)$ | M1 Dep | Their $280 \div 4(=70)$ |
|  | $£ 0.70$ or 70p | Q1 | QWC - Strand (i) - Must be in correct <br> money notation |


| 3(a) | 2 | B1 | Accept -2 |
| :--- | :--- | :--- | :--- |
| 3(b) | 16 | B1 |  |
| 3(c) | 64 | B1 |  |


| 4(a) | $-4,1$ | B1 |  |
| :---: | :--- | :---: | :--- |
| 4(b) | Marks the point $\left(-3,1 \frac{1}{2}\right)$ | B1 |  |
| 4(c) | Any point of the form $(a,-a)$ or <br> $(0,0)$ | B1 |  |


| Q Answer | Mark | Comments |
| :--- | :---: | :---: | :---: |


| 5(a) | Links all three correctly | B2 | B1 Links 2 correctly |
| :---: | :---: | :---: | :---: |
|  | Event <br> The number of the ball is <br> The number on the ball is <br> The ball is blue <br> The number on the ball is greate | an 10 | Chance of happening <br> Impossible <br> Unlikely <br> Evens <br> Likely <br> Certain |
| 5(b) | Writes two correct statements eg Event A: <br> The ball... is pink <br> The ball... is more than 100 <br> Event B: <br> The ball ... is numbered 1 to 100 <br> The ball... is yellow or blue | B2 | B1 Writes one correct statement |
| 5(c) | $\frac{1}{100}$ | B1 | oe |
| 5(d) | Tries to find the factors of an odd number <br> or multiplication of 2 primes with a correct answer | M1 | Number must be non-prime Allow 1 factor missing |
|  | 9, 25 or 49 | A1 |  |


| Q | Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |


| $\mathbf{6 ( a )}$ | 6 | B1 |  |
| :--- | :--- | :---: | :--- |
| $\mathbf{6}$ (b) | $4 y=15+11$ or $4 y=26$ | M1 | or $26 \div 4$ |
|  | 6.5 | A1 | oe |
| $\mathbf{6 ( c )}$ | $6 w+24(=18)$ | M1 | $w+4=18 \div 6$ |
|  | -1 | A1 |  |


| 7(a)(i) | $\frac{1}{9}$ | B2 | B1 For equivalent unsimplified fraction <br> eg $\frac{4}{36}$ or $\frac{2}{18}$ <br> or correct simplification of <br> their fraction to its lowest form |
| :--- | :--- | :---: | :--- |
| 7(a)(ii) | $\frac{3}{36}$ | B1 ft | oe <br> ft From an incorrect denominator in (a) |
| 7(b) | Finds at least five correct scores or <br> correct combinations of numbers | $\mathrm{M1}$ | $1,3,5,9,15,25,27,45,75,125$ |
|  | 10 | A1 |  |


| 8(a) | Shades B apart from intersection <br> with A | B1 |  |
| :---: | :--- | :---: | :--- |
| 8(b) | $A^{\prime} \cap B^{\prime}$ or (A U B)' | B1 |  |
| 8(c) | 3 letters in P only, 3 letters in <br> intersection, 4 letters in Q only | B2 | $2,4,3$, letters, 1 outside <br> $1,5,2$, letters, 2 outside <br> $0,6,1$, letters, 3 outside |
|  |  | B1 6 letters in P or 7 letters in Q <br> Numbers in correct sections <br> All correct, but other letters used |  |


| Q | Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |


| *9 | $\frac{1}{3}+\frac{2}{5}\left(=\frac{11}{15}\right) \text { or } \frac{4}{15}$ | M1 |  |
| :---: | :---: | :---: | :---: |
|  | 1 - their $\frac{11}{15} \quad\left(=\frac{4}{15}\right)$ and $44 \div$ their 4 or $44 \times 1.5$ | M1 | Sight of 11 <br> Their 11 may then be multiplied. |
|  | 66 | A1 |  |
|  | Addition, subtraction from 1 and division of 44 by their numerator or multiplication of 44 by 1.5 <br> Sight of $\frac{11}{15}$ (or $\frac{5}{15}$ and $\frac{6}{15}$ ), $\frac{4}{15}$ and 11, with an answer given, in organised working | Q1 | QWC - Strand (iii) - To achieve a correct solution a clear and organised approach must be evident |
| Alt *9 | $\begin{aligned} & 0 . \dot{3}+0.4(=0.7 \dot{3}) \text { or } \\ & 0.2 \dot{6} \end{aligned}$ | M1 | $\begin{aligned} & 33 . \dot{3} \%+40 \% ~(=73 . \dot{3} \%) \text { or } \\ & 26 . \dot{6} \% \end{aligned}$ |
|  | 1 - their 0.73 and <br> $44 \div$ their $0.2 \dot{6}(\times 0.4)$ or <br> Sight of 165 | M1 | 100 - their 73.3 and $44 \div$ their $26 . \dot{6}(\times 40)$ or Sight of 1.65 |
|  | 66 | A1 |  |
|  | Must see addition, subtraction from 1 (or 100 ) and division of 44 by their decimal (or percentage) <br> Sight of $0.7 \dot{3}, 0.2 \dot{6}$ and 165 with an integer answer <br> Sight of $73 . \dot{3}, 26 . \dot{6}$ and $1()$.65 with an integer answer | Q1 | QWC - Strand (iii) - To achieve a correct solution a clear and organised approach must be evident |

## Section B

| Q | Answer |  |  |
| :---: | :--- | :---: | :---: |
| Mark |  |  | Comments |
| 10(a)(i) | 180000 | B1 |  |
| 10(a)(ii) | 18000 | B1 |  |
| 10(a)(iii) | 1800000 | B1 |  |
| 10(b) | 2 | B1 |  |


| 11 | $20 \div 4(=5)$ | M1 | oe eg $0.25 \times 20$ <br> Can be indicated on diagram |
| :---: | :--- | :---: | :--- |
|  | Their $15 \div 2(=7.5)$ <br> or their 7 and 8 <br> or 2 pairs of numbers adding to <br> their 15 | M1 | Attempt to allocate pieces on the diagram |
|  | 7 | A1 | SC2 8 and no working |


| 12 | 1 and 3 for John | B4 | B4 All correct |
| :---: | :---: | :---: | :---: |
|  | 2 and 6 for Lily |  | B3 4 correct |
|  | 4 and 7 for Karl |  | B2 3 correct |
|  | 5 and 10 for Ruby, 8 and 9 for Leon |  | B1 2 correct or (1, 3) for John |


| 13 | Links all three correctly | B2 | B1 For 1 or 2 correct |
| :---: | :---: | :---: | :---: |


| Q | Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |
| 14 | Writes down at least 3 of the next ten multiples of 9 | M1 | $99,108,117, \ldots .$ <br> Allow 1 error in adding on a 9 <br> The multiples can be implied from (eg) $9+9,1+0+8,1+1+7$, etc |
|  | Writes down all the next ten multiples of 9 | A1 | $99,108,117,126,135,144,153,162$ $171,180$ <br> The multiples can be implied from (eg) $9+9, \quad 1+0+8,1+1+7$, etc |
|  | 1 | A1ft | ft From M1A0 if 10 multiples are given with one arithmetic error. <br> SC1 99 (does not work) |
| 15(a) | 40-10 done first | B1 | Didn't divide first |
| 15(b)(i) | $\div-$ | B1 |  |
| 15(b)(ii) | $-\times$ | B1 |  |
| 16(a) | 0.14 | B1 | oe |
| 16(b) | 25 or 8 | M1 |  |
|  | 200 | A1 |  |
| 16(c) | Common denominator with at least one numerator correct | M1 | $\frac{20}{35}+\frac{21}{35}$ |
|  | $\frac{41}{35}$ | A1 |  |
|  | 1 $\frac{6}{35}$ | B1 ft | Correct change from improper fraction |


| 17(a) | $3 x(2 x+3)$ | B2 | B1 For $3\left(2 x^{2}+3 x\right)$ or $x(6 x+9)$ |
| :---: | :--- | :---: | :--- |
| $\mathbf{1 7 ( b )}$ | $4 x+24(-x)(=3 x+24)$ | M1 | $3 x+3 a$ or $(3 x+) 24=(3 x+) 3 a$ |
|  | $3(x+8)$ or $(a=) 8$ | A1 | Q1 |
|  | Expansion, simplification and <br> solution <br> Shows $3 x+24$ and $(a=) 8$ | QWC - Strand (ii) - Logical algebraic steps <br> to a solution <br> Allow one arithmetic error |  |


| $\mathbf{Q}$ | Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |


| 18(a)(i) | $y=3$ | B1 | oe |
| :---: | :---: | :---: | :---: |
| 18(a)(ii) | $x=-1$ | B1 | oe <br> SC1 $x=3$ in (a)(i) and $y=-1$ in (a)(ii) <br> or <br> $y=-1$ in (a)(i) and $x=3$ in (a)(ii) |
| 18(b)(i) | Either point marked at $(-1,-1)$ or $(3,3)$ | M1 | Point may be implied by their line going through it |
|  | Correct line drawn crossing $L$ and $M$ | A1 |  |
| 18(b)(ii) | $y=x$ | B1 ft | ft Their line if not vertical or horizontal |


| 19 | $[-2.8,-2.6]$ and $[0.6,0.8]$ | B2 | B1 For either <br> SC1 $[-2.9,-2.8]$ and $[0.8,0.9]$ or <br> $[-2.4,-2.3]$ and $[0.3,0.4]$ |
| :---: | :--- | :---: | :---: |


| 20(a) | $n+1$ | B1 |  |
| :--- | :--- | :---: | :--- |
| 20(b) | $n+1+n+2=5 n$ <br> or $2 n+3=5 n$ | B2 | B1 For a correct LHS or RHS expression |

