## GCSE <br> MATHEMATICS

Specimen 2015
Morning
Time allowed: 1 hour 30 minutes

## Materials

## For this paper you must have:

- mathematical instruments

You may not use a calculator


## Instructions

- Use black ink or black ball-point pen. Draw diagrams in pencil.
- Fill in the boxes at the bottom of this page.
- Answer all questions.
- You must answer the questions in the space provided. Do not write outside the box around each page or on blank pages.
- Do all rough work in this book. Cross through any work that you do not want to be marked.
- In all calculations, show clearly how you work out your answer.


## Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 80 .
- You may ask for more answer paper, graph paper and tracing paper. These must be tagged securely to this answer booklet.

Please write clearly, in block capitals, to allow character computer recognition.
Centre number $\square$ Candidate number $\square$
Surname $\square$
Forename(s) $\square$

Candidate signature $\qquad$

Answer all questions in the spaces provided.

1 (a) Circle the smallest number.
2.3
2.3
2.33
2.03

1 (b) Circle the largest number.
2.3
2.3
2.33
2.03

2 Here is a sequence.
40
35
30
25
20

Circle the expression for the $n$th term of the sequence.
$5 n+35$
$5 n-45$
$45-5 n$
$n-5$

3 Which of these is not a square number?
Circle your answer.
$4 \times 10^{2}$
$4 \times 10^{6}$
$9 \times 10^{3}$
$9 \times 10^{4}$
$4 \quad$ Work out $\quad 64.32 \div 0.12$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$ $\longrightarrow$

Answer

Turn over for the next question

5 The scatter graph shows the number of driving lessons and the number of tests needed to pass by 10 people.

Number of tests needed to pass


5 (a) Describe the correlation.
Circle your answer.
[1 mark]
strong positive weak positive weak negative strong negative

5 (b) Use a line of best fit to estimate the number of tests needed to pass by a person who has 50 lessons.
$\qquad$
$\qquad$
$\qquad$

Answer

5 (c) Meera says,
"I can use the trend to predict the number of driving tests needed to pass for any number of driving lessons."

Comment on her statement.
$\qquad$
$\qquad$
$\qquad$
$6 \quad$ Which of $\frac{2}{5}$ or $\frac{5}{8}$ is closer in value to $\frac{1}{2}$ ?
You must show your working
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer $\qquad$

## Turn over for the next question

7 A shape is made from rectangles.
7 (a) On the diagram below shade an area represented by the expression $a d+c d$


7 (b) On the diagram below shade the area represented by the expression $d(a+2 c)$ [1 mark]


7 (c) Write down an expression for the area of the whole shape.


Answer
$8 \quad$ Circle the value of $\quad \cos 30^{\circ}$
$\frac{1}{\sqrt{3}}$
$\frac{1}{2}$
$\frac{\sqrt{3}}{2}$
$\frac{2}{\sqrt{3}}$

## Turn over for the next question

$9 \quad$ Alan, Ben and Carl ran a 1000 metre race.
The distance-time graph shows the race.


9 (a) Who won the race?
Give a reason for your answer.

Answer $\qquad$

Reason

9 (b) Describe the race.

Turn over for the next question

10

$$
\begin{aligned}
2 x+3 y & =15.5 \\
x+y & =6
\end{aligned}
$$

Work out the values of $x$ and $y$.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

$$
x=
$$

$\qquad$

$$
y=
$$

11 Five integers have
a mode of 6
a median of 8
a mean of 10
What is the greatest possible range of the five integers?
You must show your working.
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer

12 Write $2(7 x+4)-4(x+6)+1$ in the form $a(b x+c)$
where $a, b$ and $c$ are integers and $a>1$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer

Turn over for the next question

13
Here is a map of France.


Scale: 1 cm represents 80 km

13 (a) Estimate the time it would take to drive from Paris to Marseille.
Assume

- the road is straight
- an average speed of $100 \mathrm{~km} / \mathrm{h}$

13 (b) Comment on how each assumption affects the accuracy of your estimate.

Assumption 1
$\qquad$
$\qquad$

Assumption 2

14 The pilot of an aircraft wants to fly from $A$ to $D$.
The aircraft flies from $A$ to $E, 1^{\circ}$ off course.
Not drawn accurately


14 (a) The distance $B C$ is 1 mile.
Work out the distance $D E$.

14 (b) How should the aircraft have turned at $C$ to fly directly towards $D$ ?
Tick a box.


15 The shape is rotated $90^{\circ}$ clockwise about point $A$.
It is then enlarged by scale factor -2 , centre $B$.
Draw the final shape on the diagram.


16 Rearrange $y=\frac{4-3 x}{x-5}$ to make $x$ the subject.

Answer

17 The diagram shows a rectangle inside a semicircle.
The rectangle has dimensions 16 cm by 6 cm
Not drawn
 accurately

Work out the shaded area.
Give your answer in terms of $\pi$.

18 Two straight lines are shown. $B$ is the midpoint of $A C$.
$T B: B S=2: 3$


Work out the coordinates of $T$.
[4 marks]
$\qquad$
$\qquad$ $\longrightarrow$
$\qquad$
$\qquad$
$\qquad$

Answer ( $\qquad$ , $\qquad$

19 A cuboid has dimensions $x \mathrm{~cm}, x \mathrm{~cm}$ and $y \mathrm{~cm}$

$x$ is increased by $10 \%$
$y$ is decreased by $20 \%$
Work out and describe the percentage change in the volume of the cuboid.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer
$20 \quad$ Circle the value of $\quad 9^{-\frac{1}{2}}$

$$
\begin{array}{llll}
\frac{1}{81} & \frac{1}{3} & -3 & -4 \frac{1}{2}
\end{array}
$$

21 Expand and simplify $(2 x+5)(2 x-5)(3 x+7)$
$\qquad$ $\longrightarrow$ $\longrightarrow$ L___
$\qquad$
$\qquad$
$\qquad$ $\longrightarrow$
$\qquad$
$\qquad$

Answer

22 Write $\frac{26}{\sqrt{2}}-\frac{12}{\sqrt{18}}+2 \sqrt{50}$ in the form $a \sqrt{2}$ where $a$ is an integer.

Answer

23 (a) The graph of $y=\sin x$ is shown for $0^{\circ} \leqslant x \leqslant 360^{\circ}$ On the grid sketch the graph of $\quad y=\sin x-1$ for $0^{\circ} \leqslant x \leqslant 360^{\circ}$


23 (b) The graph of $y=\sin x$ is shown on the grid for $0^{\circ} \leqslant x \leqslant 360^{\circ}$
On this grid sketch the graph of

$$
y=-\sin x \text { for } 0^{\circ} \leqslant x \leqslant 360^{\circ}
$$



23 (c) On this grid sketch the graph of $y=\tan x$ for $0^{\circ} \leqslant x \leqslant 360^{\circ}$


Turn over for the next question

24 A bag contains $n$ beads.
One bead is black and the rest are white.
Two beads are taken from the bag at random.

24 (a) Show that the probability that both beads are white is $\frac{n-2}{n}$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

24 (b) The probability that both beads are white is greater than 0.9 Work out the least possible value of $n$.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer
$25 \quad A B C D$ is a parallelogram.
$A B E$ is a straight line and $A B: B E=3: 2$
$B C$ and $E D$ intersect at $F$.

$$
\overrightarrow{A B}=\mathbf{a} \text { and } \overrightarrow{A D}=\mathbf{b}
$$

Not drawn accurately


25 (a) Work out $\overrightarrow{E D}$ in terms of $\mathbf{a}$ and $\mathbf{b}$.
Give your answer in its simplest form.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer

25 (b) Deduce $\overrightarrow{E F}$ in terms of $\mathbf{a}$ and $\mathbf{b}$.

There are no questions printed on this page

DO NOT WRITE ON THIS PAGE ANSWER IN THE SPACES PROVIDED

