

General Certificate of Education

Mathematics 6360

MM03 Mechanics 3

Mark Scheme

2008 examination - June series

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Μ	mark is for method				
m or dM	mark is dependent on one or more M marks and is for method				
А	mark is dependent on M or m marks and is for accuracy				
В	mark is independent of M or m marks and is for method and accuracy				
E	mark is for explanation				
$\sqrt{10}$ or ft or F	follow through from previous				
	incorrect result	MC	mis-copy		
CAO	correct answer only	MR	mis-read		
CSO	correct solution only	RA	required accuracy		
AWFW	anything which falls within	FW	further work		
AWRT	anything which rounds to	ISW	ignore subsequent work		
ACF	any correct form	FIW	from incorrect work		
AG	answer given	BOD	given benefit of doubt		
SC	special case	WR	work replaced by candidate		
OE	or equivalent	FB	formulae book		
A2,1	2 or 1 (or 0) accuracy marks	NOS	not on scheme		
–x EE	deduct x marks for each error	G	graph		
NMS	no method shown	с	candidate		
PI	possibly implied	sf	significant figure(s)		
SCA	substantially correct approach	dp	decimal place(s)		

Key to mark scheme and abbreviations used in marking

No Method Shown

Where the question specifically requires a particular method to be used, we must usually see evidence of use of this method for any marks to be awarded. However, there are situations in some units where part marks would be appropriate, particularly when similar techniques are involved. Your Principal Examiner will alert you to these and details will be provided on the mark scheme.

Where the answer can be reasonably obtained without showing working and it is very unlikely that the correct answer can be obtained by using an incorrect method, we must award **full marks**. However, the obvious penalty to candidates showing no working is that incorrect answers, however close, earn **no marks**.

Where a question asks the candidate to state or write down a result, no method need be shown for full marks.

Where the permitted calculator has functions which reasonably allow the solution of the question directly, the correct answer without working earns **full marks**, unless it is given to less than the degree of accuracy accepted in the mark scheme, when it gains **no marks**.

Otherwise we require evidence of a correct method for any marks to be awarded.

MM03

MM03				-	
Q	Solution		Marks	Total	Comments
1	$LT^{-1} = L^{\alpha} \times (ML^{-3})^{\beta} (LT^{-2})^{\gamma}$		M1		
	There is no <i>M</i> on the left hand side,		E1		
	so $\beta = 0$.		EI		
	$LT^{-1} = L^{\alpha + \gamma} T^{-2\gamma}$		m1		Dependent on M1
	$\alpha + \gamma = 1$ $-2\gamma = -1$		1		
			m1		Equating corresponding indices
	$\gamma = \frac{1}{2}$		A1		
	$\alpha = \frac{1}{2}$		A1	6	
	2				
2 (a)		Total		6	
2 (a)	$_{A}v_{B} = v_{B} - v_{A}$		M1		
	= (3i+4j) - (5i-j)		A1	2	
	=-2i+5j				
(b)	$_{A}r_{0B} = (40i - 90j) - (-60i + 160j)$		M1		Simplification not
	=100i - 250j				Simplification not necessary
	$_{A}r_{B} = (100i - 250j) + (-2i + 5j)t$		m1 A1F		
			AII	3	
					ALTERNATIVE :
					$r_A = (60i + 160j) + (5i - j)t$ M1
					$r_{B} = (40i - 90j) + (3i + 4j)t$
					$_{A}r_{B} = [(40i - 90j) + (3i + 4j)t] -$
					$\left[\left(60i + 160j \right) + \left(5i - j \right) t \right] m1A1$
(c)					
	$_{A}r_{B} = (100 - 2t)i + (-250 + 5t)j$		M1		Collecting <i>i</i> and <i>j</i> terms
	$(100 - 2t) = 0 \Leftrightarrow t = 50$		A1F		
	$(-250+5t) = 0 \Leftrightarrow t = 50$			3	
	\therefore A and B would collide.		E1	5	
				ALTE	RNATIVE:
					$2t)i + (-250 + 5t)j] \cdot (-2i + 5j) = 0$ M1
					$4t - 1250 + 25t = 0 \implies t = 50$ A1
				$ _{A}r_{B} ($	$\overline{100 - 2 \times 50)^2 + (-250 + 5 \times 50)^2} = 0$
					ad <i>B</i> would collide E1
		Total		8	
				0	

MINI03 (cont	Solution	Monka	Total	Commonto
Q	Solution	Marks	Total	Comments
3	$\int_{0}^{t} 5 \times 10^{3} t^{2} dt = 0.2(2) - 0.2(0)$	M1A1		Impulse-Momentum principle
	$\frac{5 \times 10^3}{3} t^3 = 0.4$	A1F		
	t = 0.0621	A1F	4	At least 3 sig. fig. required
	Total		4	
4(a)	C.L.M. $m (4\mathbf{i} + 3\mathbf{j}) + 2m(-2\mathbf{i} + 2\mathbf{j}) = mv + 2m(\mathbf{i} + \mathbf{j})$ $7\mathbf{j} = v + (2\mathbf{i} + 2\mathbf{j})$	M1		
	$v = -2\mathbf{i} + 5\mathbf{j}$	A2,1,0	3	A1 for one slip
(b)	The angle with j direction : A: $\tan^{-1}\frac{2}{5} = 21.8^{\circ}$			OE. in i direction
	$B: \tan^{-1}\frac{1}{1} = 45^{\circ}$	M1		M1 for two inverse tan and addition of angles
	The angle = $21.8^{\circ} + 45^{\circ} = 67^{\circ}$	A1F	3	AWRT. Alternative (not in the specification) $(-2\mathbf{i}+5\mathbf{j}).(\mathbf{i}+\mathbf{j}) = \sqrt{29} \times \sqrt{2} \cos \theta$ (M1)
				$\cos\theta = \frac{3}{\sqrt{58}} \tag{A1}$
				$\theta = 67^{\circ}$ (A1F) awrt
(c)	The impulse = Gain in momentum of A = $m(-2\mathbf{i} + 5\mathbf{j}) - m(4\mathbf{i} + 3\mathbf{j})$ = $-6m\mathbf{i} + 2m\mathbf{j}$	M1 A1F A1F	3	
(d)	$-3\mathbf{i} + \mathbf{j}$ or any scalar multiple of $-3\mathbf{i} + \mathbf{j}$	B1	1	
	Total		10	

MM03 (cont Q	Solution	Marks	Total	Comments
5(a)	$5 = 10 \cos \alpha t$	M1		
	$t = \frac{5}{10\cos\alpha}$	A1		
	$1 = -\frac{1}{2}(9.8)t^2 + 10\sin\alpha t$	M1A1		
	$1 = -\frac{1}{2}(9.8)\frac{25}{100\cos^2\alpha} + 10\sin\alpha\frac{5}{10\cos\alpha}$	m1		Dependent on both M1s
	$1 = -\frac{1}{2}(9.8)\frac{25}{100}(1 + \tan^2 \alpha) + 10\sin \alpha \frac{5}{10\cos \alpha}$	A1		
	$49\tan^2\alpha - 200\tan\alpha + 89 = 0$	A1	7	Answer given
(b)	$\tan \alpha = \frac{200 \pm \sqrt{40000 - 4(49)(89)}}{2 \times 49}$	M1		
	= 3.57, 0.508	A1	2	AWRT
	$\alpha = 74.4^{\circ}, 26.9^{\circ}$	A1F	3	
(c)(i)	$10\cos 26.9^\circ = 8.92$ (or 8.91) > 8			
	\Rightarrow The can will be knocked off the wall	M1		Both values checked
	$10\cos74.4^{\circ} = 2.69 < 8$	A1F		Acc. of both results
	\Rightarrow The can will not be knocked off the wall	E1	3	Correct conclusions
		The can $10 \cos \alpha$ $\cos \alpha > 0$ $\alpha < 36.9$ So, for α	x > 8 0.8 0° $\alpha = 26.9$	M1A1 The can will be knocked off E1
5(c)(ii)	x = ut	und for	$\alpha = 71.1$	
	$t = \frac{5}{10\cos 26.9^\circ}$			
	$v = 10\sin 26.9^{\circ} - 9.8(\frac{5}{10\cos 26.9^{\circ}})$	M1		Any correct use of equations
	v = -0.970	A1F		
	$\tan\theta = \frac{-0.970}{8.92}$	M1		
	$\theta = -6.2^{\circ}$			
	At an angle of depression of 6.2°	A1F	4	AWRT 6°
	Total		17	

Q	Solution	Marks	Total	Comments
6(a)	v la u			
	Parallel to the wall : velocity is unchanged $u \cos \alpha = v \sin \alpha$ Perpendicular to the wall : Law of Restitution	M1		
	$\frac{v\cos\alpha}{u\sin\alpha} = \frac{3}{4}$	M1		
	$\frac{v\cos\alpha}{v\tan\alpha\sin\alpha} = \frac{3}{4}$	m1		Dependent on both M1s
	$\frac{\cos^2\alpha}{\sin^2\alpha} = \frac{3}{4}$	m1		Dependent on both M1s
	$\tan^2 \alpha = \frac{4}{3}$			
(b)	$\tan \alpha = \frac{2}{\sqrt{3}}$	A1	5	Answer given
	$v = \frac{u}{\tan \alpha}$	M1		
	$v = \frac{\sqrt{3}}{2}u$ or 0.866 <i>u</i>	A1	2	
(c)	Magnitude of Impulse = Change in momentum perpendicular to the wall	M1		
	$= 0.2 \times v \cos \alpha - (-0.2 \times 4 \sin \alpha)$	A1 A1		
	$= 0.2 \times \frac{\sqrt{3}}{2} \times 4\cos\alpha + 0.2 \times 4\sin\alpha$	m1		
	= 1.06 Ns	A1F		
	Average Force = $\frac{1.06}{0.1}$ = 10.6 N	A1F	6	
	Total		13	

MM03 (con Q	Solution	Marks	Total	Comments
7	y y y y y y y y y y			
(a)	$v_y^2 = u^2 \sin^2 \theta - 2 \operatorname{gcos} \alpha . y$	M1 A1		
	$0 = u^2 \sin^2 \theta - 2g \cos \alpha y_{\max}$	m1		
	$y_{\max} = \frac{u^2 \sin^2 \theta}{2g \cos \alpha}$	A1F	4	
(b)(i)	$u\sin\theta t - \frac{1}{2}g\cos(\alpha)t^2 = 0$	M1		
	$t = \frac{2u\sin\theta}{g\cos\alpha}$	A1	2	
(ii)	$x = u\cos\theta t - \frac{1}{2}g\sin(-\alpha)t^2$	M1 A1		
	$R = u\cos\theta(\frac{2u\sin\theta}{g\cos\alpha}) + \frac{1}{2}g\sin\alpha(\frac{2u\sin\theta}{g\cos\alpha})^2$	M1		
	$=\frac{2u^2\cos\theta\sin\theta\cos\alpha+2u^2\sin\alpha\sin^2\theta}{g\cos^2\alpha}$	m1		Dependent on both M1s
	$=\frac{2u^2\sin\theta(\cos\theta\cos\alpha+\sin\theta\sin\alpha)}{g\cos^2\alpha}$	A1F		19115
	$=\frac{2u^2\sin\theta\cos(\theta-\alpha)}{g\cos^2\alpha}$	A1	6	Answer given
(iii)	$\overline{OP} = \frac{2u^2 \sin \theta \cos(\theta - \alpha)}{g \cos^2 \alpha}$			
	$=\frac{2u^2 \frac{1}{2} \left[\sin(2\theta - \alpha) + \sin\alpha\right]}{g \cos^2 \alpha}$	M1A1		
	\overline{OP} is max when $\sin(2\theta - \alpha) = 1$	M 1		
	$\overline{OP}_{\max} = \frac{u^2 \left(1 + \sin \alpha\right)}{g \cos^2 \alpha}$	A1F		
	$\overline{OP}_{\max} = \frac{u^2 (1 + \sin \alpha)}{g (1 - \sin^2 \alpha)}$			
	$\overline{OP}_{\max} = \frac{u^2}{g\left(1 - \sin\alpha\right)}$	A1	5	Answer given
	Total		17	

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Q	Solution	Marks	Total	Comments
7(a)	ALTERNATIVE			
	$0 = u\sin\theta - g\cos a t$	M1		
	$t = \frac{u\sin\theta}{g\cos a}$	A1		
	$y_{max} = u\sin\theta \left(\frac{u\sin\theta}{g\cos a}\right) - \frac{1}{2}g\cos a \left(\frac{u\sin\theta}{g\cos a}\right)^2$	m1		
	$y_{max} = \frac{u^2 \sin^2 \theta}{2g \cos a}$	A1F	4	
	Total		4	